

The Pennsylvania System of School Assessment

Mathematics Item and Scoring Sampler



2021* Grade 3

^{*} This is a revised version of the 2017 Item and Scoring Sampler.

TABLE OF CONTENTS

INFORMATION ABOUT MATHEMATICS

| Introduction | 1 |
|---|------|
| General Introduction | 1 |
| Pennsylvania Core Standards (PCS) | 1 |
| What Is Included | 1 |
| Purpose and Uses | 2 |
| Item Format and Scoring Guidelines | 2 |
| Item Alignment | 2 |
| Testing Time and Mode of Testing Delivery for the PSSA | 3 |
| Mathematics Reporting Categories | 3 |
| General Description of Scoring Guidelines for Mathematics Open-Ended Question | ons4 |
| Item and Scoring Sampler Format | 5 |
| Grade 3 Ruler | 5 |
| Mathematics Test Directions | 6 |
| Multiple-Choice Items | 7 |
| Open-Ended Question | 26 |
| Item-Specific Scoring Guideline | 28 |
| Mathematics—Summary Data | 45 |

INTRODUCTION

General Introduction

The Pennsylvania Department of Education (PDE) provides districts and schools with tools to assist in delivering focused instructional programs aligned with the Pennsylvania Core Standards (PCS). These tools include Academic Standards, Assessment Anchor documents, assessment handbooks, and content-based item and scoring samplers. This Item and Scoring Sampler is a useful tool for Pennsylvania educators in preparing local instructional programs by providing samples of test item types and scored student responses. The item sampler is not designed to be used as a pretest, a curriculum, or other benchmark for operational testing.

This Item and Scoring Sampler is available in Braille format. For more information regarding Braille, call (717) 901-2238.

Pennsylvania Core Standards (PCS)

This sampler contains examples of test items (questions) designed to assess the Pennsylvania Assessment Anchors and Eligible Content aligned to the PCS. The Mathematics, Reading, and Writing PSSA transitioned to PCS-based operational Mathematics and English Language Arts assessments starting with the spring 2015 PSSA administration.

The PCS-aligned Assessment Anchors and Eligible Content documents are posted on this portal:

www.education.pa.gov [Hover over "Data and Reporting," select "Assessment and Accountability," and select "PSSA-PA System of School Assessment." Then select "Assessment Anchors/Eligible Content" on the right side of the screen.]

What Is Included

This sampler contains test questions (items) that have been written to be aligned with the Assessment Anchors, which are aligned to the PCS. The test questions provide an idea of the types of items that will appear on an operational, PCS-based PSSA. Each sample test question has been through a rigorous review process to ensure alignment with the Assessment Anchors.

Typically an item and scoring sampler is released every year to provide students and educators with a resource to assist in delivering focused instructional programs aligned to the PCS. However, due to the cancellation of standardized testing in 2019–2020, the 2021 Item and Scoring Sampler is a revised version of the previously released 2017 Item and Scoring Sampler. This revised version ensures that students and educators have an enhanced item and scoring sampler to use during instruction and/or preparation of students to take the PSSA Exam.

Purpose and Uses

The items in this sampler may be used¹ as examples for creating assessment items at the classroom level, and they may also be copied and used as part of a local instructional program. Classroom teachers may find it beneficial to have students respond to the open-ended (OE) item in this sampler. Educators can then use the sampler as a guide to score the responses either independently or together with colleagues within a school or district.

Item Format and Scoring Guidelines

The multiple-choice (MC) items have four answer choices. Each correct response to an MC item is worth one point.

Each OE item is designed to take approximately ten to fifteen minutes to complete. During the administration of the PSSA, students are given additional time as necessary to complete the test items. Each OE item in mathematics is scored using an item-specific scoring guideline based on a 0–4-point scale. In this sampler, every item-specific scoring guideline is combined with examples of student responses that represent each score point to form a practical, item-specific scoring guide.

This sampler also includes the *General Description of Scoring Guidelines for Mathematics Open-Ended Questions* that students will have access to during a PSSA mathematics administration. The general description of scoring guidelines may be distributed to students for use during local assessments and may also be used by educators when scoring local assessments.¹

Item Alignment

All PSSA items are aligned to statements and specifications included in the *Assessment Anchors* and *Eligible Content Aligned to the Pennsylvania Core Standards*. The mathematics content, process skills, directives, and action statements included in the PSSA mathematics questions align with the Assessment Anchor Content Standards. The Eligible Content statements represent the limits of the content of the mathematics questions.

¹ The permission to copy and/or use these materials does not extend to commercial purposes.

Testing Time and Mode of Testing Delivery for the PSSA

The PSSA is delivered in traditional paper-and-pencil format as well as in an online format. The estimated time to respond to a test question is the same for both methods of test delivery. During an official testing administration, students are given additional time as necessary to complete the test questions. The following table shows the estimated response time for each item type.

| Mathematics Item Type | MC | OE |
|-----------------------------------|----|----------|
| Estimated Response Time (minutes) | 2 | 10 to 15 |

Mathematics Reporting Categories

The Assessment Anchors are organized into four classifications as listed below.

| • | A = Numbers and Operations | • | C = Geometry |
|---|----------------------------|---|-----------------------------------|
| • | B = Algebraic Concepts | • | D = Data Analysis and Probability |

These four classifications are used throughout the grade levels. In addition to these classifications, there are five Reporting Categories for each grade level. The first letter of each Reporting Category represents the classification; the second letter represents the Domain as stated in the Common Core State Standards for Mathematics. Listed below are the Reporting Categories for Grade 3.

- A-T = Numbers and Operations in Base Ten
- A-F = Numbers and Operations—Fractions
- B-O = Operations and Algebraic Thinking
- C-G = Geometry
- D-M = Measurement and Data

Examples of MC and OE items assessing these categories are included in this sampler.

General Description of Scoring Guidelines for Mathematics Open-Ended Questions

4—The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

3—The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

2—The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1—The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.
- 0—The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.

| BLK (blank) | ls blank, is entirely erase | d, or gives a writ | ten refusal to resp | ono |
|-------------|-----------------------------|--------------------|---------------------|-----|
| OT | ls off-task | | | |

LOE.....ls in a language other than English

Special Categories within zero reported separately:

IL.....ls illegible

Item and Scoring Sampler Format

This sampler includes the test directions and scoring guidelines that appear in the PSSA Mathematics assessments. Each MC item is followed by a table that includes the alignment, the answer key, the depth of knowledge (DOK) level, the percentage² of students who chose each answer option, and a brief answer-option analysis or rationale. The OE item is followed by a table that includes the item alignment, DOK level, and mean student score. Additionally, each of the included item-specific scoring guidelines is combined with sample student responses representing each score point to form a practical, item-specific scoring guide. The *General Description of Scoring Guidelines for Mathematics Open-Ended Questions* used to develop the item-specific scoring guidelines should be used if any additional item-specific scoring guidelines are created for use within local instructional programs.

Example Multiple-Choice Item Information Table

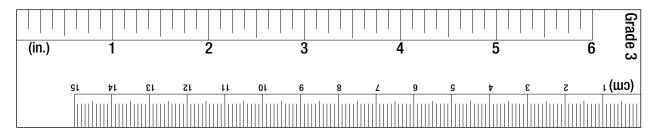
| Item Information | |
|--------------------|---|
| Alignment | Assigned AAEC |
| Answer Key | Correct Answer |
| Depth of Knowledge | Assigned DOK |
| p-value A | Percentage of students who selected this option |
| p-value B | Percentage of students who selected this option |
| p-value C | Percentage of students who selected this option |
| p-value D | Percentage of students who selected this option |
| Option Annotations | Brief answer-option analysis or rationale |

Example Open-Ended Item Information Table

| Alignment |
|-----------|
|-----------|

Grade 3 Ruler

The ruler shown below is not intended to be used to measure. It has been included as a representation of the rulers that will be provided for students when they take the test. Due to differences in printers, the ruler and measurement questions within this sampler may not accurately reproduce to scale.



² All *p*-value percentages listed in the item information tables have been rounded.

Mathematics Test Directions

Directions: On the following pages are the Mathematics questions.

- You may not use a calculator on this test.
- You may need a ruler for question(s) on this test.

Directions for Multiple-Choice Questions

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

Directions for Open-Ended Questions

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example, if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you may use the space provided, but only those parts of your response that the question specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the booklet. Some answers may require graphing, plotting, labeling, drawing, or shading.
 If you use scratch paper, be sure to transfer your final response and any needed work or reasoning to the booklet.

MULTIPLE-CHOICE ITEMS

1. Alex is painting the chairs in a classroom.

So far he has painted 3 of the 8 chairs in the classroom.

Which statement correctly compares the fraction of painted chairs to the fraction of unpainted chairs?

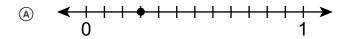
- (B) $\frac{5}{8} < \frac{3}{8}$
- (a) $\frac{8}{5} < \frac{8}{3}$

| Item Information | |
|--------------------|---|
| Alignment | A-F.1.1.1 |
| | A-F.1.1.5 |
| Answer Key | A |
| Depth of Knowledge | 2 |
| p-value A | 68% (correct answer) |
| p-value B | 16% |
| p-value C | 10% |
| p-value D | 6% |
| Option Annotations | A. Correct: identifies the comparison symbol as "less than" and orders the fractions based on the numerators (3 and 5) while identifying the common denominator to represent the whole (8 chairs in the classroom) B. sets up the fractions correctly but reverses the comparison C. uses reciprocals of the fractions and compares denominators D. uses reciprocals of the fractions but compares correctly |

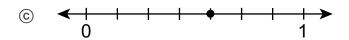
2. Matt measured a peg from one of his games.

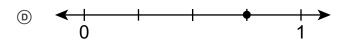
The peg was $\frac{3}{4}$ inch in length.

Which number line shows the length, in inches, of Matt's peg?









| Item Information | |
|--------------------|--|
| Alignment | A-F.1.1.2 |
| | A-F.1.1.3 |
| Answer Key | D |
| Depth of Knowledge | 1 |
| p-value A | 15% |
| p-value B | 16% |
| p-value C | 10% |
| p-value D | 59% (correct answer) |
| Option Annotations | A. plots a point at the third mark of a number line divided into twelfths (3 × 4) B. plots a point so there are 3 marks before and 4 marks after C. plots a point so there are 4 marks before and 3 marks after D. Correct: plots a point at the third mark of a number line divided into fourths |

3. Maddox has a jar with $\frac{2}{6}$ ounce of peanut butter in it.

Which fraction is equal to the amount of peanut butter in the jar?

- (A) $\frac{1}{3}$ ounce
- $\bigcirc B \qquad \frac{2}{3} \text{ ounce}$
- © $\frac{1}{6}$ ounce

| Item Information | | |
|--------------------|---|--|
| Alignment | A-F.1.1.3 | |
| Answer Key | A | |
| Depth of Knowledge | 1 | |
| p-value A | 41% (correct answer) | |
| p-value B | 22% | |
| p-value C | 20% | |
| p-value D | 17% | |
| Option Annotations | A. Correct: divides both numerator and denominator by 2 B. divides only the denominator by 2 C. divides only the numerator by 2 D. multiplies denominator by numerator OR doubles denominator without doubling numerator | |

4. Tim put 12 pictures into his scrapbook.

He filled each page with 3 pictures.

Which expression shows the number of pages Tim filled?

- A 3 ÷ 12
- ⊕ 4 ÷ 12
- © 12 ÷ 4
- D 12 ÷ 3

| Item Information | | |
|--------------------|---|--|
| Alignment | B-O.1.1.2 | |
| Answer Key | D | |
| Depth of Knowledge | 1 | |
| p-value A | 15% | |
| p-value B | 4% | |
| p-value C | 6% | |
| p-value D | 75% (correct answer) | |
| Option Annotations | A. reverses the numbers | |
| | B. reverses the numbers and uses the number of pages instead of the number of pictures per page | |
| | C. uses the number of pages as the divisor instead of the number of pictures per page | |
| | D. Correct: writes an expression to divide the number of pictures (12) by the number of pictures per page (3) | |

5. The town of Smithville has 5 fire stations.

Each fire station has 4 fire trucks.

How many fire trucks does the town of Smithville have?

- <a>9
- ® 16
- © 20
- [®] 25

| Item Information | |
|--------------------|---|
| Alignment | B-O.1.2 |
| Answer Key | С |
| Depth of Knowledge | 1 |
| p-value A | 15% |
| p-value B | 4% |
| p-value C | 78% (correct answer) |
| p-value D | 3% |
| Option Annotations | A. adds the values B. multiplies 4 by 4 C. Correct: multiplies the number of fire stations (5) by the number of fire trucks (4) at each station D. multiplies 5 by 5 |

6. Ethan has 2 pencil boxes.

Each pencil box has 7 pencils in it.

The total number of pencils Ethan has can be expressed as 2×7 .

What is another way to show the number of pencils Ethan has?

- A 7 ÷ 2
- B 7 x 2
- © 7 + 2
- D 7 2

| Item Information | |
|--------------------|--|
| Alignment | B-O.2.1.1 |
| Answer Key | В |
| Depth of Knowledge | 1 |
| p-value A | 14% |
| p-value B | 79% (correct answer) |
| p-value C | 6% |
| p-value D | 1% |
| Option Annotations | A. selects division instead of multiplication B. Correct: recognizes that, when multiplying, numbers may be switched without changing the value of the expression (commutative property of multiplication) C. selects addition (which is also commutative) instead of multiplication D. selects subtraction instead of multiplication |

7. Joan puts 42 cherries into 6 bowls.

She puts the same number of cherries into each bowl.

The number of cherries in each bowl can be found using the equation shown below.

$$6 \times ? = 42$$

How many cherries are in each bowl?

- A
- B 5
- © 6
- D 7

| Item Information | | | |
|--------------------|--|--|--|
| Alignment | B-O.2.2.1 | | |
| | B-O.1.2 | | |
| Answer Key | D | | |
| Depth of Knowledge | 1 | | |
| p-value A | 6% | | |
| p-value B | 4% | | |
| p-value C | 10% | | |
| p-value D | 80% (correct answer) | | |
| Option Annotations | A. mixes up 42 with 24 (4 \times 6 = 24) | | |
| | B. thinks $5 \times 6 = 42$; wrong multiple of 6 | | |
| | C. thinks $6 \times 6 = 42$; wrong multiple of 6 | | |
| | D. Correct: recalls that $6 \times 7 = 42$ OR relates the missing number | | |
| | equation to the division problem 42 ÷ 6 | | |

8. Some friends are having a picnic at a park.

They take 5 cars to the park.

There are 4 people in each car.

Each person will eat 2 sandwiches at the picnic.

How many sandwiches in total will the friends eat at the picnic?

- A 11
- B 20
- © 22
- 40

| Item Information | | |
|--------------------|--|--|
| Alignment | B-O.3.1.1 | |
| Answer Key | D | |
| Depth of Knowledge | 2 | |
| p-value A | 17% | |
| p-value B | 16% | |
| p-value C | 9% | |
| p-value D | 58% (correct answer) | |
| Option Annotations | A. adds numbers in the problem B. selects number of people going to the park C. multiplies 5 by 4, then adds 2 instead of multiplying by 2 D. Correct: finds the number of people by multiplying 5 by 4 and then finds the number of sandwiches by multiplying the number of people (20) by 2 | |

- **9.** Which story matches the equation $3 \times 12 4 = \square$?
 - A Kelsey buys 3 pieces of gum. She buys 12 more pieces of gum. She gives away 4 pieces of gum. How many pieces of gum does Kelsey have now?
 - ® Kelsey buys 3 packs of gum.
 Each pack has 4 pieces of gum.
 She gives away 12 pieces of gum.
 How many pieces of gum does Kelsey have now?
 - © Kelsey buys 3 packs of gum.
 Each pack has 12 pieces of gum.
 She gives away 4 pieces of gum.
 How many pieces of gum does Kelsey have now?
 - Melsey buys 12 packs of gum.
 Each pack has 4 pieces of gum.
 She gives away 3 pieces of gum.
 How many pieces of gum does Kelsey have now?

| Item Information | | | |
|--------------------|---|--|--|
| Alignment | B-O.3.1.6 | | |
| Answer Key | С | | |
| Depth of Knowledge | 2 | | |
| p-value A | 24% | | |
| p-value B | 5% | | |
| p-value C | 67% (correct answer) | | |
| p-value D | 4% | | |
| Option Annotations | A. selects a story that matches 3 + 12 - 4 = ? B. selects a story that matches 3 × 4 - 12 = ? C. Correct: selects a story that matches multiplying 3 by 12 before subtracting 4 D. selects a story that matches 12 × 4 - 3 = ? | | |

10. Chris went outside to play at 3:20 P.M.

He came back inside at 4:05 P.M.

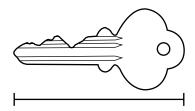
How many minutes was Chris outside?

- A 15
- ® 25
- © 45
- [®] 60

| Item Information | | | |
|--------------------|---|--|--|
| Alignment | D-M.1.1.2 | | |
| Answer Key | C | | |
| Depth of Knowledge | 1 | | |
| p-value A | 8% | | |
| p-value B | 13% | | |
| p-value C | 67% (correct answer) | | |
| p-value D | 12% | | |
| Option Annotations | A. subtracts 5 from 20 B. adds 5 to 20 C. Correct: identifies the time from 3:20 to 4:00 as 40 minutes and the time from 4:00 to 4:05 as 5 more minutes, and then adds 5 to 40 D. looks only at the hour | | |

11. Maria's house key is shown below.

House Key



Use your ruler to measure the length of Maria's house key.

Which measurement is **closest** to the length of Maria's house key?

- \bigcirc $\frac{3}{4}$ inch
- ® 1 inch
- © $1\frac{3}{4}$ inches
- 2 inches

| Alignment | D-M.1.2.3 | |
|--------------------|---|--|
| Answer Key | С | |
| Depth of Knowledge | 1 | |
| p-value A | 6% | |
| p-value B | 3% | |
| p-value C | 49% (correct answer) | |
| p-value D | 42% | |
| Option Annotations | A. selects only the fractional part of the measurement | |
| | B. selects only the whole number part of the measurement | |
| | C. Correct: measures the length as $\frac{3}{4}$ inch beyond 1 inch | |
| | D. selects the whole number closest to the actual length | |

12. Rounded to the nearest dollar, Aziza spent \$12.00 on snacks while visiting the zoo.

Which could be the exact amount of money Aziza spent on snacks?

- A \$11.47
- ® \$11.58
- © \$12.54
- \$12.61

| Item Information | | |
|--------------------|--|--|
| Alignment | D-M.1.3.3 | |
| Answer Key | В | |
| Depth of Knowledge | 2 | |
| p-value A | 13% | |
| p-value B | 61% (correct answer) | |
| p-value C | 16% | |
| p-value D | 10% | |
| Option Annotations | A. looks at hundredths place (last digit) to decide whether to round up or down B. Correct: looks at the digit to the right of the dollars place (5) and recognizes that the value should be rounded up to the next dollar OR identifies a dollar amount in the interval \$11.50–\$12.49 (all the values that round to \$12) OR recognizes that, among the four choices, \$11.58 is closest to \$12 C. uses "if 5 or less, then round down" as the rounding rule instead of "if 5 or greater, then round up" D. rounds down | |

13. Workers at an apple orchard picked four different types of apples.

They recorded the numbers of bushels of apples picked in the graph below.

Apples Picked at the Orchard

| Туре | Number of Bushels Picked |
|--------|--|
| Empire | ÓÓÓÓÓ |
| Gala | ÓÓÓÓ |
| Rome | ÓÓÓÓÓÓÓ |
| York | ()()()()()()()()()()()()()()()()()()() |

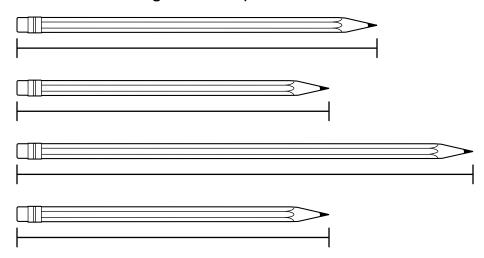
Key: = 5 bushels

How many fewer bushels of Empire apples than York apples were picked?

- A
- B 5
- © 8
- [®] 15

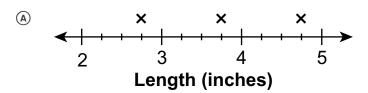
| Item Information | | |
|--------------------|---|--|
| Alignment | D-M.2.1.2 | |
| Answer Key | D | |
| Depth of Knowledge | 2 | |
| p-value A | 24% | |
| p-value B | 9% | |
| p-value C | 5% | |
| p-value D | 62% (correct answer) | |
| Option Annotations | A. finds the difference between the number of "apples" but does not apply the key B. does not apply the key and counts the "apples" for Empire C. does not apply the key and counts the "apples" for York D. Correct: applies the key to determine the number of bushels of Empire apples (5 × 5 = 25) and subtracts that value from the number of bushels of York apples (8 × 5 = 40) OR finds the difference between the number of "apples" (8 - 5 = 3) and applies the key to the difference (3 × 5 = 15) | |

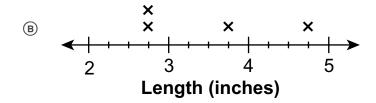
14. Jonathan measured the lengths of his pencils.

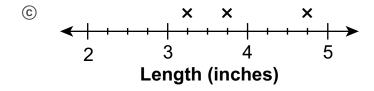


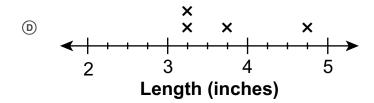
Use your ruler to measure the lengths, in inches, of the pencils.

Which line plot shows the lengths of Jonathan's pencils?









| Item Information | | |
|--------------------|---|--|
| Alignment | D-M.2.1.3 | |
| Answer Key | D | |
| Depth of Knowledge | 2 | |
| p-value A | 11% | |
| p-value B | 23% | |
| p-value C | 14% | |
| p-value D | 52% (correct answer) | |
| Option Annotations | A. marks $3\frac{1}{4}$ as $2\frac{3}{4}$, does not include the second pencil of this length | |
| | B. marks $3\frac{1}{4}$ as $2\frac{3}{4}$ | |
| | C. does not include the second $3\frac{1}{4}$ -inch pencil | |
| | D. Correct: measures the shortest pencils as $3\frac{1}{4}$ inches and includes | |
| | both measurements | |

15. The tally chart below shows the number of students who chose each type of seed for a science experiment.

Science Experiment

| Type of Seed | Number of Students |
|--------------|--------------------|
| bean | |
| mustard | Ш |
| sunflower | #1 |

Which pictograph also shows the number of students who chose each type of seed for the science experiment?

A Science Experiment

| Type of Seed | Number of Students |
|--------------|-----------------------|
| bean | †† |
| mustard | 1 |
| sunflower | † † |
| • | |

Key: \uparrow = 2 students

B

Science Experiment

| Type of Seed | Number of Students |
|--------------|-----------------------|
| bean | |
| mustard | 1 |
| sunflower | |

Key: \uparrow = 2 students

©

Science Experiment

| Type of Seed | Number of Students |
|-----------------|-----------------------|
| bean | ^ |
| mustard | † † † |
| sunflower | *** |

Key: • = 2 students

(D)

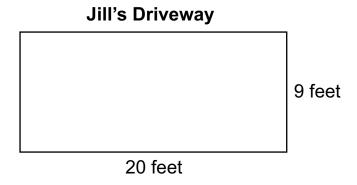
Science Experiment

| Type of Seed | Number of Students |
|--------------|--------------------|
| bean | |
| mustard | † |
| sunflower | |

Key: \uparrow = 2 students

| Item Information | | |
|--------------------|--|--|
| Alignment | D-M.2.1.4 | |
| Answer Key | В | |
| Depth of Knowledge | 2 | |
| p-value A | 3% | |
| p-value B | 62% (correct answer) | |
| p-value C | 33% | |
| p-value D | 2% | |
| Option Annotations | A. switches amounts for bean and sunflower B. Correct: applies the key to each row, using a half figure for the odd tally C. does not apply key (uses 1 figure = 1 student) D. uses only whole figures (does not use the half figure for mustard) | |

16. Jill's driveway is in the shape of the rectangle shown below.



What is the perimeter of Jill's driveway?

- A 29 feet
- [®] 58 feet
- © 180 feet
- 360 feet

| Item Information | | |
|--------------------|---|--|
| Alignment | D-M.4.1.1 | |
| Answer Key | В | |
| Depth of Knowledge | 1 | |
| p-value A | 26% | |
| p-value B | 60% (correct answer) | |
| p-value C | 12% | |
| p-value D | 2% | |
| Option Annotations | A. adds the side lengths that are labeled but does not double the sum B. Correct: adds all four side lengths (20 + 9 + 20 + 9) OR adds the side lengths that are labeled and then doubles the sum C. multiplies the side lengths that are labeled OR confuses the rules for area and for perimeter D. uses multiplication (instead of addition) before doubling the result | |

THIS PAGE IS INTENTIONALLY BLANK.

OPEN-ENDED QUESTION

17. Ms. Baker's class visited the zoo.

The table below shows the weights of the animals the class saw at the zoo.

Animal Weights

| Animal | Weight (pounds) |
|------------|-----------------|
| panda | 275 |
| polar bear | 849 |
| sloth bear | 291 |

| A. | LIST the weights, in pounds, of the animals in order from lightest to heaviest. | | |
|----|---|----------|--|
| | lightest | heaviest | |
| | | | |

Together, the sloth bear and the panda weigh less than the polar bear.

B. How many pounds less is their combined weight than the polar bear's weight?

PUT your answer in the **BLANK BELOW**.

SHOW or **EXPLAIN** all your work.

Answer: _____ pounds

Go to the next page to finish question 17.

GO ON

17. Continued. Please refer to the previous page for task explanation.

Ms. Baker asked her students to round the polar bear's weight to the greatest place value. One student explained that the polar bear's weight rounds to 900 because in the number 849, the 9 is bigger than 5, and if a number is 5 or bigger, then the number should be rounded up. C. **EXPLAIN** the mistake this student made.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.



Item-Specific Scoring Guideline

#17 Item Information

| Alignment | A-T.1 | Depth of Knowledge | 2 | Mean Score | 1.79 |
|-----------|-------|-----------------------|---|------------|------|
|-----------|-------|-----------------------|---|------------|------|

Assessment Anchor this item will be reported under:

M03.A-T.1—Use place-value understanding and properties of operations to perform multi-digit arithmetic.

Specific Anchor Descriptor addressed by this item:

M03.A-T.1.1 — Apply place-value strategies to solve problems.

Scoring Guide

| Score | In this item, the student |
|-------|---|
| 4 | Demonstrates a thorough understanding of how to use place-value understanding and properties of operations to perform multi-digit arithmetic by computing accurately and fluently and making reasonable estimates. |
| 3 | Demonstrates a general understanding of how to use place-value understanding and properties of operations to perform multi-digit arithmetic by computing accurately and fluently and making reasonable estimates. |
| 2 | Demonstrates a partial understanding of how to use place-value understanding and properties of operations to perform multi-digit arithmetic by computing accurately and fluently and making reasonable estimates. |
| 1 | Demonstrates minimal understanding of how to use place-value understanding and properties of operations to perform multi-digit arithmetic by computing accurately and fluently and making reasonable estimates. |
| 0 | The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question. |

Top-Scoring Student Response and Training Notes

| Score | Description | |
|-------|---|--|
| 4 | Student earns 4 points. | |
| 3 | Student earns 3.0–3.5 points. | |
| 2 | Student earns 2.0–2.5 points. | |
| 1 | Student earns 0.5–1.5 points. OR Student demonstrates minimal understanding of how to use place-value understanding and properties of operations to perform multi-digit arithmetic. | |
| 0 | Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured. | |

Top-Scoring Response

Part A (1 point):

1 point for correct answer

| What? | Why? |
|----------------------------------|------|
| <u>275</u> <u>291</u> <u>849</u> | |

Part B (2 points):

- 1 point for correct answer
- 1 point for correct support

 $OR \frac{1}{2}$ point for correct but incomplete support

| What? | Why? |
|--------------|--|
| 283 (pounds) | Sample Work: 291 + 275 = 566 849 - 566 = 283 OR Sample Explanation: First I found the combined weight of the sloth bear and the panda by adding their weights (291 + 275). To find how much less they weigh than the polar bear, I subtracted the combined weight (566) from the polar bear's weight (849) to get 283 pounds. |

Part C (1 point):

1 point for complete explanation

 $OR\frac{1}{2}$ point for correct but incomplete explanation

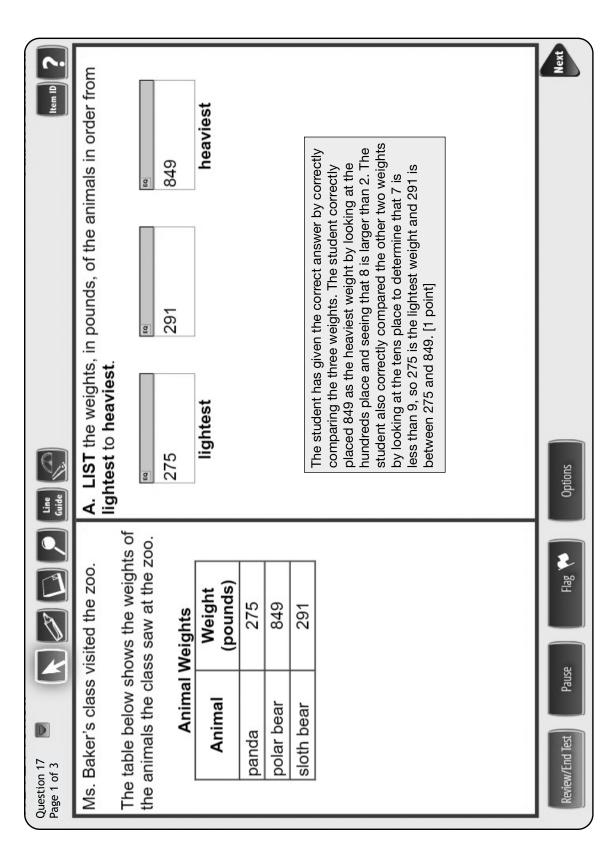
| What? | Why? | |
|-------|---|--|
| | Sample Explanation: The student looked at the 9, which is in the ones place. To round to the greatest place value, the student needs to look at the 4, which is in the tens place. Since 4 is smaller than 5, the number rounds to 800 and not 900. | |

STUDENT RESPONSE

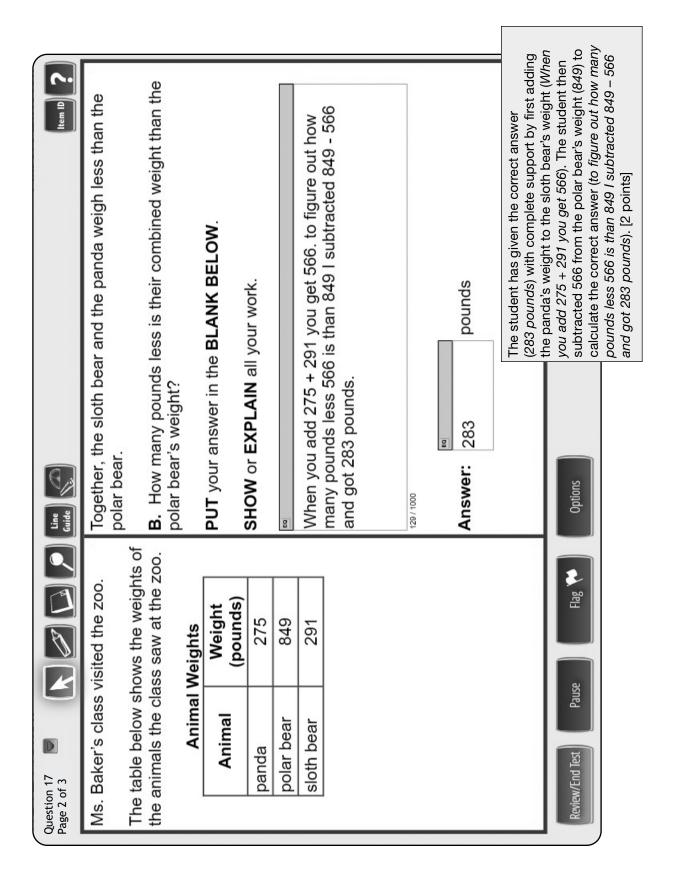
Response Score: 4 points



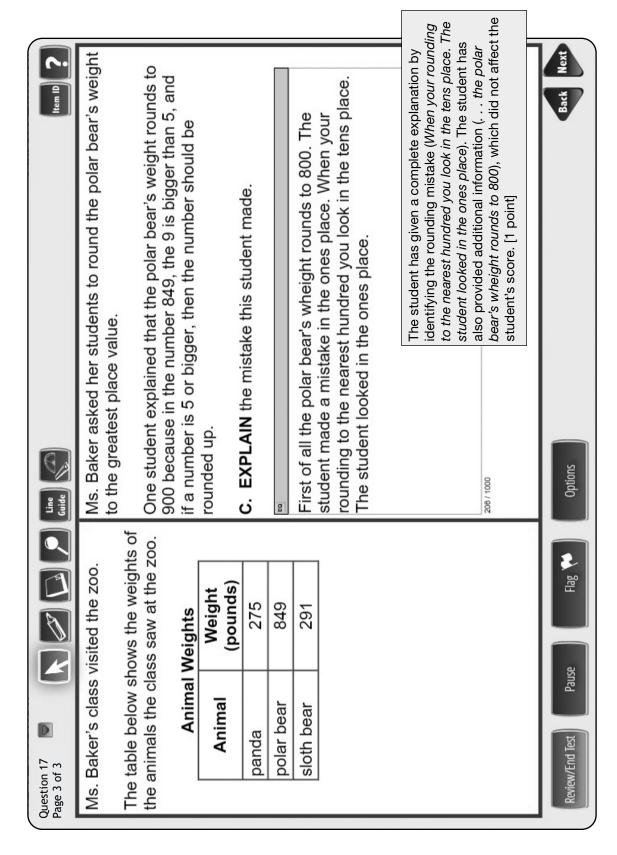
PART A



PART B



PART C



STUDENT RESPONSE

Response Score: 3 points

17. Ms. Baker's class visited the zoo.

The table below shows the weights of the animals the class saw at the zoo.

Animal Weights

| Animal | Weight (pounds) |
|------------|-----------------|
| panda | 275 |
| polar bear | 849 |
| sloth bear | 291 |

A. LIST the weights, in pounds, of the animals in order from **lightest** to **heaviest**.

275

29

849

lightest heaviest

The student has given the correct answer by correctly comparing the three weights. [1 point] Please see annotation A on page 35 for complete details.

Together, the sloth bear and the panda weigh less than the polar bear.

B. How many pounds less is their combined weight than the polary bear's weight?

PUT your answer in the BLANK BELOW. +291 - 566SHOW or EXPLAIN all your work. -566 - 283

It is less than because 849-566=283 so the polar bear weighs more.

Answer: 285 pounds

The student has given the correct answer (283 pounds) with complete support by showing work adding the panda's weight (275) to the sloth bear's weight (291) to get a total of 566. [2 points]

PSSA Grade 3 Mathematics Item and Scoring Sampler - September 2021

17. Continued. Please refer to the previous page for task explanation.

Ms. Baker asked her students to round the polar bear's weight to the greatest place value.

One student explained that the polar bear's weight rounds to 900 because in the number 849, the 9 is bigger than 5, and if a number is 5 or bigger, then the number should be rounded up.

C. EXPLAIN the mistake this student made.

The mistake is that it is not 4 it is 5 so it should be rounded to 850 not 900.

A: The student has given the correct answer by correctly comparing the three weights. The student correctly placed 849 as the heaviest weight by looking at the digits in the hundreds place and seeing that 8 is larger than 2. The student also correctly compared the other two weights by looking at the digits in the tens place to determine that 7 is less than 9, so 275 is the lightest weight and 291 is between 275 and 849. [1 point]

B: The student has given the correct answer ($283 \ pounds$) with complete support by showing work adding the panda's weight (275) to the sloth bear's weight (291) to get a total of 566. The student then subtracted 566 from the polar bear's weight (849) to calculate the correct answer of 283 pounds. The student also included an explanation (849 - 566 = 283 so the polar bear weighs more), however, the explanation alone would have been considered incomplete support, since it does not also address how 566 was derived. [2 points]

C: The student has given an incorrect explanation by not rounding to the correct greatest place value. The student incorrectly rounded to the tens place instead of the hundreds place (it is not 4 it is 5 so it should be rounded to 850 not 900). [0 points]

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

STOP

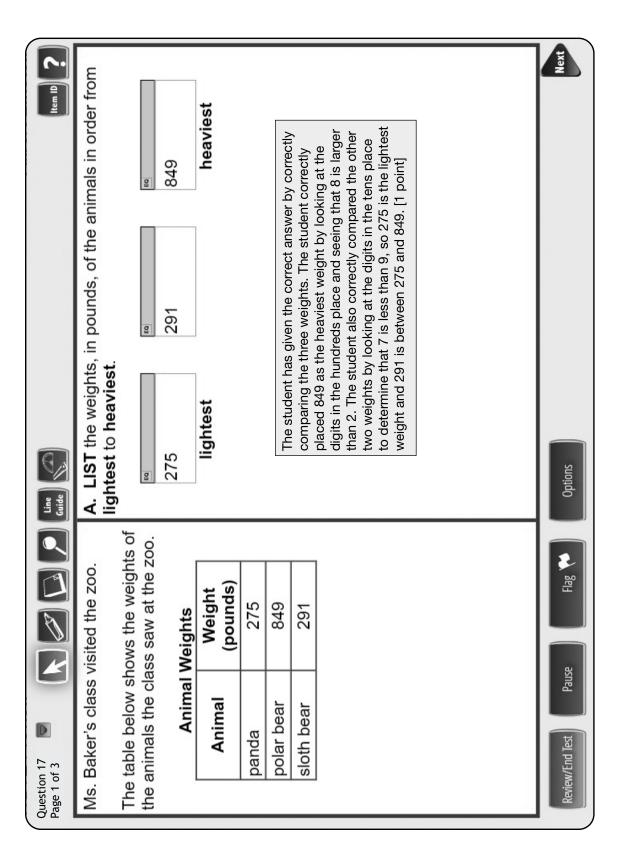
PSSA MATHEMATICS GRADE 3

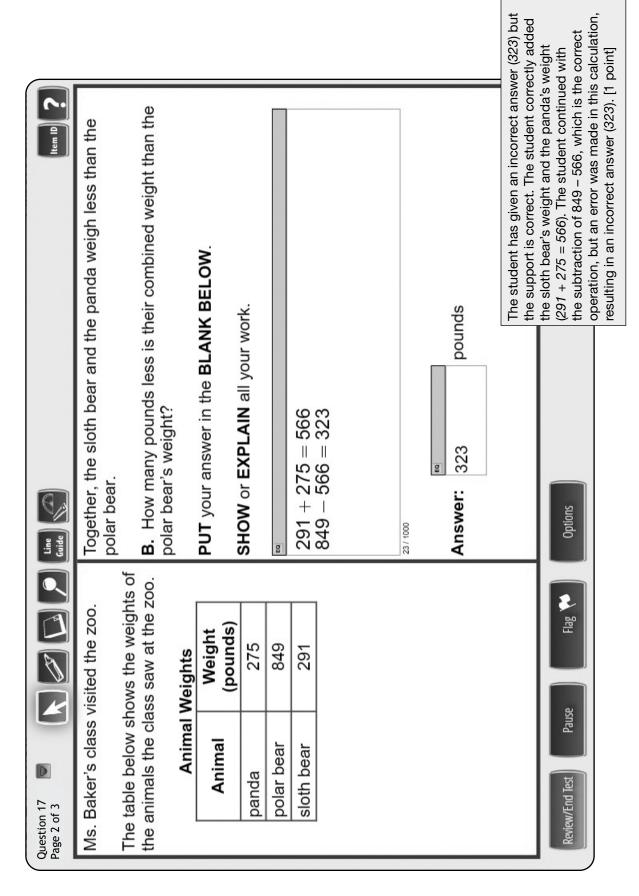
STUDENT RESPONSE

Response Score: 2 points

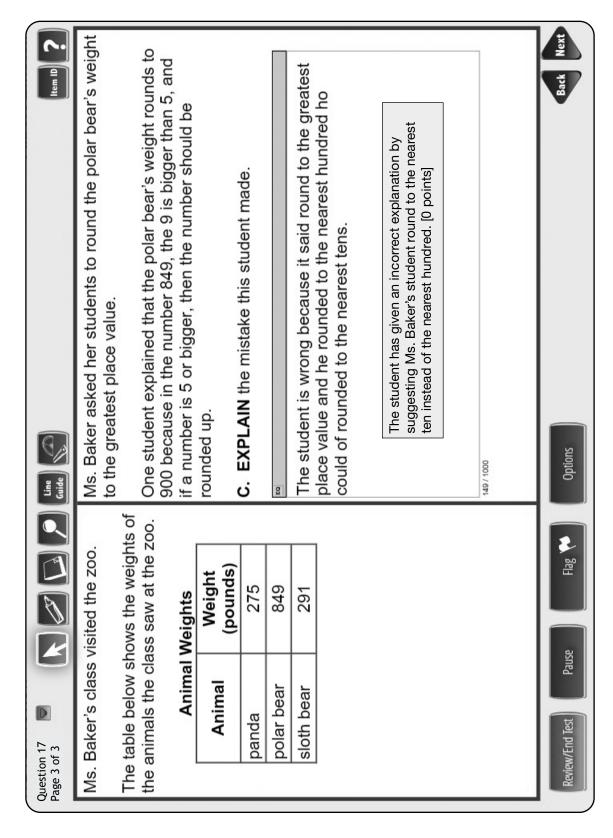


PART A





PART C



THIS PAGE IS INTENTIONALLY BLANK.

STUDENT RESPONSE

Response Score: 1 point

17. Ms. Baker's class visited the zoo.

The table below shows the weights of the animals the class saw at the zoo.

Animal Weights

| Animal | Weight (pounds) | | | | |
|------------|-----------------|--|--|--|--|
| panda | 275 | | | | |
| polar bear | 849 | | | | |
| sloth bear | 291 | | | | |

A. LIST the weights, in pounds, of the animals in order from **lightest** to **heaviest**.

275

291

849

lightest

heaviest

The student has given the correct answer by correctly comparing the three weights. [1 point] **Please see annotation A on page 41 for complete details.**

Together, the sloth bear and the panda weigh less than the polar bear.

B. How many pounds less is their combined weight than the polar bear's weight?

PUT your answer in the BLANK BELOW.

SHOW or **EXPLAIN** all your work.

+275

Answer: 666 pounds

The student has given an incorrect answer (666 pounds) with correct but incomplete support. [0.5 points] Please see annotation B on page 41 for complete details.

17. Continued. Please refer to the previous page for task explanation.

Ms. Baker asked her students to round the polar bear's weight to the greatest place value.

One student explained that the polar bear's weight rounds to 900 because in the number 849, the 9 is bigger than 5, and if a number is 5 or bigger, then the number should be rounded up.

C. EXPLAIN the mistake this student made.

because ther are is no 5 in 849 there is a 8 in 849 but no 5.

A: The student has given the correct answer by correctly comparing the three weights. The student correctly placed 849 as the heaviest weight by looking at the digits in the hundreds place and seeing that 8 is larger than 2. The student also correctly compared the other two weights by looking at the digits in the tens place to determine that 7 is less than 9, so 275 is the lightest weight and 291 is between 275 and 849. [1 point]

B: The student has given an incorrect answer ($666 \ pounds$) with correct but incomplete support. The student's support shows a correct first step for Part B by adding the weights of the panda and the sloth bear (275 + 291 = 566). The student does not go on to subtract the combined weights (566) from the polar bear's weight (849). [0.5 points]

C: The student has given an incorrect explanation that does not explain the mistake made by Ms. Baker's student. [0 points]

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

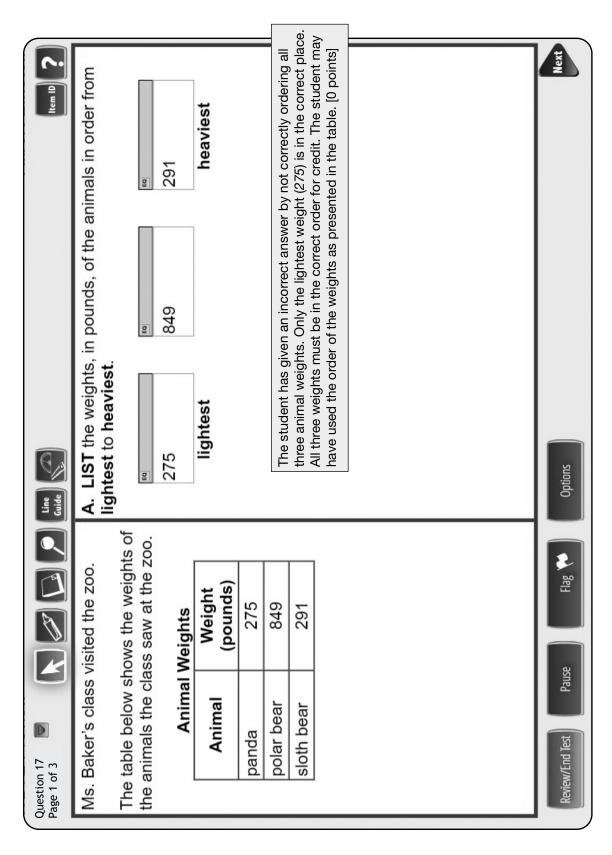


STUDENT RESPONSE

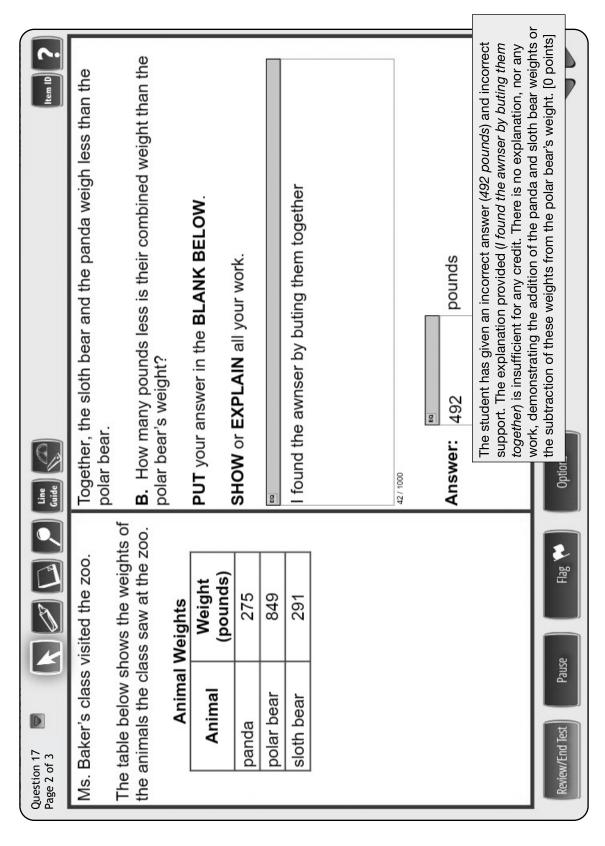
Response Score: 0 points



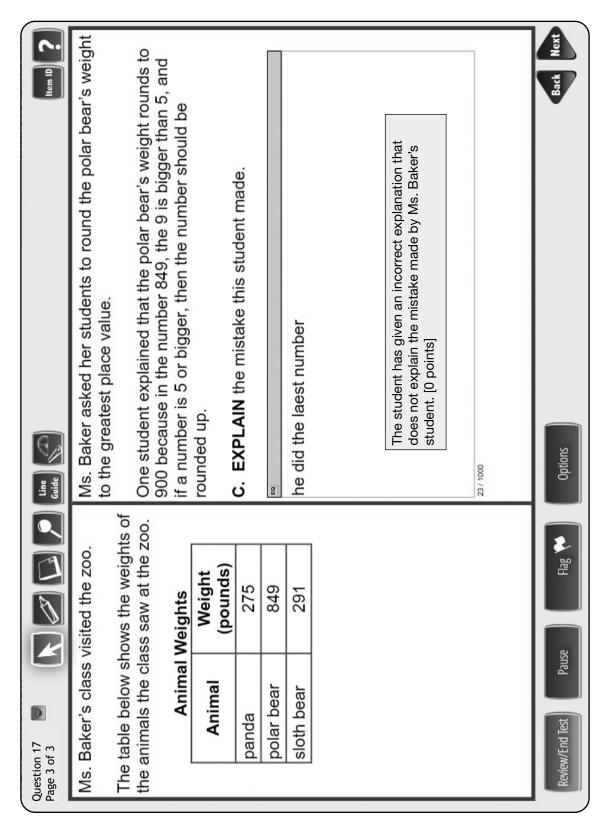
PART A



PART B



PART C



PSSA MATHEMATICS GRADE 3

MATHEMATICS—SUMMARY DATA

Multiple-Choice

| Sample Number | Alignment | Answer Key | Depth of Knowledge | <i>p</i> -value A | <i>p</i> -value B | <i>p</i> -value C | <i>p</i> -value D |
|------------------|------------------------|------------|-----------------------|----------------------|----------------------|----------------------|----------------------|
| 1 | A-F.1.1.1 A-F.1.1.5 | А | 2 | 68% | 16% | 10% | 6% |
| 2 | A-F.1.1.2 A-F.1.1.3 | D | 1 | 15% | 16% | 10% | 59% |
| 3 | A-F.1.1.3 | А | 1 | 41% | 22% | 20% | 17% |
| 4 | B-O.1.1.2 | D | 1 | 15% | 4% | 6% | 75% |
| 5 | B-O.1.2 | С | 1 | 15% | 4% | 78% | 3% |
| 6 | B-O.2.1.1 | В | 1 | 14% | 79% | 6% | 1% |
| 7 | B-O.2.2.1 B-O.1.2 | D | 1 | 6% | 4% | 10% | 80% |
| 8 | B-O.3.1.1 | D | 2 | 17% | 16% | 9% | 58% |
| 9 | B-O.3.1.6 | С | 2 | 24% | 5% | 67% | 4% |
| 10 | D-M.1.1.2 | С | 1 | 8% | 13% | 67% | 12% |
| 11 | D-M.1.2.3 | С | 1 | 6% | 3% | 49% | 42% |
| 12 | D-M.1.3.3 | В | 2 | 13% | 61% | 16% | 10% |
| 13 | D-M.2.1.2 | D | 2 | 24% | 9% | 5% | 62% |
| 14 | D-M.2.1.3 | D | 2 | 11% | 23% | 14% | 52% |
| 15 | D-M.2.1.4 | В | 2 | 3% | 62% | 33% | 2% |
| 16 | D-M.4.1.1 | В | 1 | 26% | 60% | 12% | 2% |

Open-Ended

| Sample Number | Alignment | Points | Depth of Knowledge | Mean Score |
|------------------|-----------|--------|-----------------------|------------|
| 17 | A-T.1 | 4 | 2 | 1.79 |

PSSA Grade 3 Mathematics Item and Scoring Sampler

Copyright © 2021 by the Pennsylvania Department of Education. The materials contained in this publication may be duplicated by Pennsylvania educators for local classroom use. This permission does not extend to the duplication of materials for commercial use.